



**CALIFORNIA STATE SCIENCE FAIR  
2009 PROJECT SUMMARY**

<b>Name(s)</b> Sundeep Bekal	<b>Project Number</b> <b>S1602</b>
<b>Project Title</b> <b>A Study of Dandelin Spheres: A Second Year Investigation</b>	
<b>Abstract</b>	
<b>Objectives/Goals</b> The purpose of this investigation is to see if there is a relationship that forms between the radius of the smaller dandelin sphere to the tangent of the angle RLM and distances that form inside the ellipse.	
<b>Methods/Materials</b> I investigated a conic section of an ellipse that contained two Dandelin Spheres to determine if there was such a relationship. I used the same program as last year, Geometer's Sketchpad, to generate measurements of last year's 2D model of the conic section so that I could better investigate the relationship. After slicing the spheres along the central pole, I looked to see if there were any patterns or relationships. To do this I set the radius of the smaller circle (sphere in 3-D) to 1.09 cm. I changed the radius by .05 cm every time while also noting how the other segments changed or did not change.	
<b>Materials</b> -Geometer's Sketchpad -Calculator -Computer -Paper -Pencil	
<b>Results</b> After looking through the data tables I noticed that the radius had the same exact values as $(a+c)(\tan(1/2) \text{ angleRLM})$ , where $(a+c)$ is the distance located in the ellipse. I also noticed that the ratio of the $(\text{radius})/(a+c)$ had the same values as $\tan((1/2) \text{ angleRLM})$ . I figured that this would be true because the $\tan(\theta) = (\text{opposite})/(\text{adjacent})$ which in this case, would be $\tan((1/2) \text{ angleRLM}) = (\text{radius})/(a+c)$ .	
<b>Conclusions/Discussion</b> Based on my research with previous experiments involving the spheres I proved that the radius of the sphere $r(s)$ will equal $(1/2 \tan)(a+c)$ , where $(a+c)$ is the distance located in the ellipse. This is only true when the ratio of $r(s)/(a+c)$ equals $(1/2 \tan)$ .  $r(s) = \tan(1/2 \theta)(a+c)$ which is only true when $\tan(1/2 \theta) = (r(s))/(a+c)$ .	
<b>Summary Statement</b> To find the relationship that forms between a dandelin sphere's radius to an angle formed by an ellipse.	
<b>Help Received</b> Teacher proofread my project	